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# On the contact interfaces between the driver and the vehicle seat

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## ABSTRACT

Automotive seating is characterized by boundary conditions which contain nonlinear contact interfaces. These interfaces experience the vibro-impacts (slaps) and frictional slips. The slaps take place in contact interfaces subjected to high amplitude vibrations, being characterized by very brief duration, rapid dissipation of energy and large accelerations and decelerations, respectively. Including of friction into the contact interface modeling improves the interaction between the driver and the vehicle seat by making the simulation more realistic. The vibro-impacts and the frictional slips can be developed simultaneously in a contact surface. As a result, the friction-induced vibrations interact with the vibrations and waves at the interface, generating sounds and instabilities. Identification of boundary conditions in the driver-seat system is performed by using the concept of the interference distance or penetration. The interference distance is introduced as an optimization problem. It is shown that the optimization problem provides robust solutions to minimum distance and interference problems.

## **INTRODUCTION**

The evaluation of comfort and discomfort of the driver depends on the interaction between the seat properties, driver characteristics, environmental conditions and the driver-seat system, respectively. When the slip and vibro-impact mechanisms are simultaneously developed, the picture of the actual normal forces of the contact interface is changed as shown by Jalali et al. [1] when investigating the micro-vibroimpacts at boundary condition of a clamped Euler-Bernoulli beam. The impact mechanism affects the frictional slip mechanism when they simultaneously develop in a contact interface. Karnopp [2] describes the friction as a function of the relative velocity, while Menq et al. [3] introduced a modified micro-slip model in terms of an elasto-plastic shear layer. Comprehensive investigations of contact friction and the vibro-impact mechanism into the contact interfaces subjected to high amplitude vibrations have been performed by Ferri [4], Berger [5], and Gilardi and Sharf [6], respectively. Returning to the automotive seating subject, we know that

the road and vehicle engines conditions are transferred into the body through the seat. Most car seats have fore- and aft adjustment as well as adjustable seat back inclination for obtaining an acceptable occupant position and also to fitting as large a range of the population as possible (Jonsson [7]). An optimal seatback with seat pan inclination according to (Harrison et al. [8]) is shown in *Figure.1*. The position of the driver in the car is important for the driving performance. However, the neck injuries in rear-end collisions are still an important problem for the society. Much research effort has been expended for understanding the impacts developing in the contact interfaces (Emaci et al. [9], Moon. and Shawand [10] and Yang and Begeman [11].



Figure 1. A generic seatback.

A continuous approach of the vibro-contact dynamics is developed in this paper by admitting an explicit relationship between contact force and deformation. In the continuous approach, there is no difference between the impact and the contact, and as a consequence, the methods of the non-impact dynamics can be used to solve the problem. Unlike the discrete formulation, the continuous approach of the vibrocontact dynamics allows for use of any friction model. The friction force can be considered as a combination of forces that resist motion during different energies conversion processes (elastic/plastic contacts viscous dissipation, fracture, and adhesion). In addition, the identification of nonlinear boundary conditions is performed by using the concept of the interference distance or penetration. This concept defines the contact force which in turn depends on the deformation at the contact interface. Generally, the impacts between bodies are defined by the condition of impenetrability (Kim [12]), because the contact can be found by checking the minimum distance between bodies. The contact point is the point where the minimum distance is reached [6] as shown in:

$$\min\left(\frac{1}{2}(p_1 - p_2)^T(p_1 - p_2)\right), \quad g_1(p_1) \le 0, g_2(p_2) \le 0, \qquad (1)$$

where  $p_1$  and  $p_2$  are the position vectors of two points on the two bodies and  $g_1$  and  $g_2$  are the bounding surface constraints. To define the contact force, the interference distance can be computed as

$$\min(-d), \quad g_1(p_1) \le -\frac{d}{2}e_1, \quad g_2(p_2) \le -\frac{d}{2}e_2,$$
 (2)

where d is the interference distance and  $e_1$  and  $e_2$  are the unit vectors.

## PROBLEM FORMULATION AND SOLUTION

The back of the driver surface is modeled as a double curved thin shell of thickness h and the principal radii of curvature  $R_1$  and  $R_2$  as shown in *Figure 2*.



# Figure 2. Reference and deformed configurations of the back of the driver shell.

The reference surface area is denoted by  $\Omega$ . An inertial frame of reference is defined by three mutually orthogonal unit

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vectors  $i_1, i_2, i_3$ . Position vector of a point of the shell can be written as

$$R(\xi_1,\xi_2,\zeta) = r_0(\xi_1,\xi_2) + u(\xi_1,\xi_2) + \zeta E_3(\xi_1,\xi_2), \qquad (3)$$

where  $\xi_1, \xi_2$  are the material coordinates (the lines of curvatures of the shell reference surface),  $\zeta$  is the material coordinate along the normal to the reference surface  $n = e_3, r_0$ is the position vector of the point  $P_0$  on the reference surface of the shell where the shell has a contact boundary condition, and u is the reference surface displacement vector.  $E_3$  is a unit vector, and  $E_1, E_2$  are the axial and transverse shearing strains develop during deformation. The unknown driver-seat contact domain  $D_c$  can be described by the Lamé curve

$$\left(\frac{x}{a}\right)^n + \left(\frac{y}{b}\right)^n = 1, \ n > 0, \tag{4}$$

where a and b are the radii of the oval shape. The parametric representation of (4) is

$$x(\theta) = a\cos^{2/n}\theta, \ y(\theta) = b\sin^{2/n}\theta.$$
 (5)

The integral motion equation is obtained by applying the Hamilton principle (Bauchau and Choi [13])

$$\int_{t_1}^{t_2} \int_{\Omega} \left\{ \delta u(\dot{g}_1 - N_{1,1} - N_{2,2}) + \delta E(\dot{g}_2 - M_{1,1} - M_{2,2} + F_c) \right\} d\Omega dt = 0,$$
(6)

where  $g_1, g_2$  are the linear and angular momentum vectors of the shell,  $N_1, N_2$  are spatial in-plane forces,  $F_c$  is the contact force,  $M_1, M_2$  are the bending moments. A constant normal force P is applied to the shell at the contact point  $P_0$ . The shell is excited by forced vibrations  $F(t) = f \sin(\omega t)$  having an arbitrary point excitation. The excitation frequency is chosen to be closer to the resonant frequencies of the spine. The nonlinear behavior can be spanned using its first nnonlinear normal modes. We suppose that each contact point permits small deflections. For large amplitude of vibrations the micro-slip and micro-vibro-impact develop in the contact interface of the shell. The associated contact force constrain  $F_c$  and the sticking constraint, respectively, are given by

$$F_{c} = \varphi_{c}(\delta, \dot{\delta}), \quad \varphi_{st}(\xi_{1c}, \xi_{2c}, \zeta_{c}, F_{t}) = 0,$$
(7)

where  $\delta$  is the local indentation function

$$\delta(\xi_{1c},\xi_{2c},\zeta_c,\xi_{1c},\xi_{2c},\zeta_c),$$

And  $\xi_{1c}, \xi_{2c}, \zeta_c$  are the components of the position vector of a contact point. So, the contact force  $F_c$  can be explicitly written as

$$F_c = A\delta^n + B\delta^p \dot{\delta}^q, \qquad (8)$$

where n, p, q and constants, the coefficient A depends on the material and the geometric properties of the bodies in contact, and B is defined with respect to the coefficient of restitution. Both coefficients also depend on the flexural and normal stiffnesses of the boundary condition. In the continuous model the damping depends on the indentation since the contact area increases with deformation. The first term in (8) represents the contact constraint expressed as a functional between the contact force  $F_c$  at the contact point coordinates  $\xi_{1c}, \xi_{2c}, \zeta_c$  and their time derivatives. Therefore, the normal

contact force  $F_c$  given by (7)<sub>1</sub> depends on the local indentation  $\delta$  (Hunt and Crossley [14]). Next, the friction  $F_t$ at the contact point during sticking can be defined as (Stronge [15])

$$F_t = C\delta_t + D\dot{\delta}_t, \tag{9}$$

where  $\delta_t$  is the tangential component of displacement at the contact point, *C* is the tangential stiffness and *D* is defined with respect to the coefficient of restitution  $0 \le e \le 1$ . The energy released during restitution  $W_r$  at the dynamical contact (impact) can be calculated as the negative work done by  $F_c$  during the collision

$$W_r = -\int F_c \dot{\delta} dt .$$
 (10)

The coefficient of restitution can be calculated from

$$e = \sqrt{\frac{W_r}{-W_c}} , \qquad (11)$$

where  $W_r$  is the energy released during restitution and  $W_c$  is the energy absorbed during compression. The unknowns of the problem are the contact vectors, the contact forces and the friction forces, respectively. These unknowns are determined by solving (6) by using the cnoidal method (Munteanu and Donescu [16]). The general solutions of (6), denoted by S, can be written in the form

$$S = S_{\rm lin} + S_{\rm nonlin} \,, \tag{12}$$

where the linear and nonlinear terms express the linear and nonlinear superposition, respectively, of cnoidal functions

$$S_{\text{lin}} = 2\sum_{k=0}^{n} \alpha_k \text{cn}^2 \left( \omega_k \zeta; m_k \right),$$

$$S_{\text{nonlin}} = \frac{\sum_{k=0}^{n} \beta_k \text{cn}^2 \left( \omega_k \zeta; m_k \right)}{1 + \sum_{k=0}^{n} \gamma_k \text{cn}^2 \left( \omega_k \zeta; m_k \right)}.$$
(13)

#### where $0 \le m_k \le 1$ are cnoidal moduli, and the

quantities  $\omega_k$ ,  $\alpha_k$ ,  $\beta_k$  and  $\gamma_k$  are depending on  $\varphi_c$  and  $\varphi_{st}$  (see Appendix). The presence of the contact with no material overlapping condition is detected by checking the minimum distance between bodies. A genetic algorithm is used to solve the constrained optimization problem (1) and (2). Figure 3 displays the contact domain  $D_c$  containing several contact

points detected on the back seat at the beginning of an impact, for high amplitude vibrations. In this figure the "contact point" 1 was chosen for the subsequent analysis. The size of the "contact point" depends on the mesh of the genetic algorithm.



Figure 3. The contact domain  $D_c$ .

**Figure 4** shows the identified contact force  $F_c$  with respect to  $\delta$  for the contact point 1, for four resonant frequencies of the spine. Certain frequencies in the range of the resonance frequency of the human body and specially the spine have been proved to cause the low back pain. The resonance frequency of the spine is about 4.75-6.25 Hz (Matsumoto and Griffin [17]). **Figure 5** shows the variation of the contact force  $F_c$  with respect to  $\delta$  at the contact point 1 for the same resonant frequencies. The variation of the friction  $F_t$  with respect to tangential component of displacement  $\delta_t$  at the contact point 1 is displayed in **Figure 6** for the same resonant frequencies.



Figure 4. Contact force  $F_c$  with respect to  $\delta$  in the contact point 1.



Figure 5. Friction force  $F_t$  with respect to  $\delta_t$  in the contact point 1.

The optimization problem provides robust solutions to minimum distance and interference problems. The time variation of the ratio between the area of the contact domain  $D_c$  and a chosen reference contact area, during the impact is

presented in *Figure 7* for the same resonant frequencies as before. When the slip and vibro-impact mechanisms are simultaneously developed, the vibro-impact modifies the size of the contact domain. As a consequence the driver-seat system is subject to elastic and/or plastic deformation with dissipation of energy. The collision between bodies is central with the mass centers on the line of impact.

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Figure 6. Friction force  $F_i$  with respect to  $\delta_i$  in the contact point 1.



Figure 7. Time variation of the contact area  $D_c$ 

## **CONCLUSIONS**

The paper is concerned on the modeling of coupled vibroimpacts and frictional slips at the boundary condition in the driver-seat system. Driver position had a double risk compared with other passenger seat positions. The contacting bodies experience contacts and vibro-impacts at multiple points simultaneously. Each contact point allows small deformations in normal and tangential directions at the contact interface. The interaction between the human and the seat occurs in a short time and exhibits energy transfer and dissipation.

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## **APPENDIX**

#### Cnoidal method (Munteanu and Donescu [16])

The general solution of the nonlinear ODE or PDE can be written in the terms of the theta function representation

$$\theta(x,t) = 2\frac{\mathrm{d}^2}{\mathrm{d}x^2}\log\Theta_n(\eta_1,\eta_2,...,\eta_n), \qquad (A1)$$

where  $\Theta$  is the *theta function* defined as

$$\Theta_{n}(\eta_{1},\eta_{2},...,\eta_{n}) = \sum_{M \in (-\infty,\infty)} \exp(i\sum_{i=1}^{n} M_{i}\eta_{i} + \frac{1}{2}\sum_{i,j=1}^{n} M_{i}B_{ij}M_{j}), \qquad (A2)$$

with n the number of degrees of freedom for a particular solution of the equation, and

$$\eta_j = k_j x - \omega_j t + \phi_j , \ 1 \le j \le N .$$
(A3)

In (A3),  $k_j$  are the wave numbers, the  $\omega_j$  are the frequencies and the  $\phi_j$  are the phases. Also we have

$$M\eta = Kx - \Omega t + \Phi,$$
  

$$M = [M_1, M_2, ..., M_n],$$
  

$$K = Mk, \ \Omega = M\omega, \Phi = M\phi.$$

The integer components in M are the integer indices in (A2). The matrix B can be decomposed in a diagonal matrix D and an offdiagonal matrix O, that is B = D + O. Further, we write the solution (A1) under the form

$$\theta(\eta) = 2 \frac{\partial^2}{\partial t^2} \log \Theta_n(\eta) = \theta_{lin}(\eta) + \theta_{int}(\eta).$$
(A4)

The first term  $\theta_{in}$  represents a linear superposition of cnoidal functions

$$\boldsymbol{\theta}_{lin} = \sum_{l=1}^{n} \alpha_l \mathrm{cn}^2 [\boldsymbol{\omega}_l t; \boldsymbol{m}_l], \qquad (A5)$$

with

$$q = \exp(-\pi \frac{K'}{K})$$
,  $K = K(m) + \int_{0}^{\pi/2} \frac{\mathrm{d}u}{\sqrt{1 - m \sin^2 u}}$ ,  $K'(m_1) = K(m)$ ,  $m + m_1 = 1$ .

The second term  $\theta_{int}$  represents a nonlinear superposition or interaction among cnoidal functions

$$2\frac{\mathrm{d}^2}{\mathrm{d}t^2}\log[1+\frac{F(t)}{G(t)}] \approx \frac{\beta_k \mathrm{cn}^2(\omega t, m_k)}{1+\gamma_k \mathrm{cn}^2(\omega t, m_k)}.$$
(A6)

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